



MATHEMATICS

0580/42

Paper 42 (Extended)

March 2017

MARK SCHEME

Maximum Mark: 130

Published

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Abbreviations

cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
SC	Special Case
nfww	not from wrong working
soi	seen or implied

Question	Answer	Marks	Part Marks
1 (a)	22.9 or 22.85 to 22.86	2	M1 for $\frac{8}{10+17+8} [\times 100]$ oe
	(b) $5635 \times \frac{17}{10+17+8}$ or better [= 2737]	2	M1 for $\frac{5635}{(10+17+8)}$
	(c) 5000	3	M2 for $5635 = k \left(1 + \frac{2.42}{100}\right)^5$ oe or B1 for $\left(1 + \frac{2.42}{100}\right)$
	(d) 9950	2	M1 for 2×2500 or 3×1650
	(e) 1.98 final answer	2	B1 for 1.976 or 1.98 not final answer or M1 for 130×0.0152
2 (a) (i)	Rotation	1	
	90° [anticlockwise] oe	1	
	(9, 5)	1	
	(ii) Translation	1	
	$\begin{pmatrix} -8 \\ -14 \end{pmatrix}$ oe	1	
	(iii) Enlargement	1	
	[sf] $\frac{1}{3}$	1	
	(-8, -2)	1	
	(b) (i) Image at (1, -3) (2, -3) (2, -5)	2	M1 for triangle correct size and orientation, wrong position or SC1 for correct reflection in $y = -x$
	(ii) $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	2	B1 for 1 correct column or row

Question	Answer	Marks	Part Marks
3			
(a)	0 0.5 oe 1.25 oe	1, 1, 1	
(b)	Fully correct smooth curve	4	B3 FT for 7 or 8 points or B2 FT for 5 or 6 points or B1 FT for 3 or 4 points
(c)	3.6 to 3.8	2	M1 for $y = 3.5$ soi
(d)	line $y = x + 1$ ruled -1.55 to -1.40 4.55 to 4.8	M1 A1 A1	If 0 scored SC1 for $y = x + 1$ stated or implied or for 2 correct values given
(e) (i)	Point plotted at (5, 5)	1	
(ii)	Tangent ruled from A	1	
(iii)	1.2 to 1.4	B2	B2 and M1 dep on reasonable attempt at tangent from (5, 5) M1 for change in y / change in x of <i>their</i> ruled line
4			
(a)	$\frac{1}{8}$ oe	3	M2 for $\frac{1}{2}\left(1 - \frac{1}{6} - \frac{1}{4} - \frac{1}{3}\right)$ oe or M1 for $\frac{1}{6} + \frac{1}{4} + \frac{1}{3}$ seen oe or idea that all sum to 1
(b)	$\frac{7}{12}$ oe	2	M1 for $\frac{1}{3} + \frac{1}{4}$ oe
(c) (i)	$\frac{1}{16}$ oe	2	M1 for $\frac{1}{4} \times \frac{1}{4}$ oe
(ii)	$\frac{2}{24}$ oe	3	M2 for $2 \times \frac{1}{6} \times \frac{1}{4}$ oe or M1 for $\frac{1}{6} \times \frac{1}{4}$ oe
(d)	12	1	

Question	Answer	Marks	Part Marks
<p>5 (a) (i)</p> <p>(ii)</p> <p>(b) (i)</p> <p>(ii)</p>	<p>$(3x-1)(x+4)$</p> <p>$\frac{1}{3}$ oe and -4</p> <p>$2 \times 2(x-4) - 2(2x+11) = (2x+11)(x-4)$ or better</p> <p>$2x^2 + 11x - 8x - 44$ or better</p> <p>$4x - 16 - 4x - 22 = 2x^2 - 8x + 11x - 44$ $2x^2 + 3x - 6 = 0$</p> <p>$\frac{-3 \pm \sqrt{(3)^2 - 4(2)(-6)}}{2 \times 2}$</p> <p>$-2.64$ and 1.14 final ans cao</p>	<p>2</p> <p>1</p> <p>M2</p> <p>B1</p> <p>A1</p> <p>2</p> <p>B1B1</p>	<p>M1 for $(3x+b)(x+c)$ with $bc = -4$ or $3c + b = 11$ or for $3x(x+4) - 1(x+4)$ or for $x(3x-1) + 4(3x-1)$</p> <p>M1 for common denom $2(2x+11)(x-4)$ seen or attempt to multiply through by denoms or for $\frac{2(x-4) - (2x+11)}{(2x+11)(x-4)} \left[= \frac{1}{2} \right]$</p> <p>or for other correct relevant 2 bracket expansion if alt method used</p> <p>correct solution reached with all brackets expanded and no errors or omissions seen</p> <p>B1 for $\sqrt{(3)^2 - 4(2)(-6)}$ or better or $\left(x + \frac{3}{4}\right)^2$ oe and B1 for $\frac{-3 + \sqrt{q}}{2(2)}$ or $\frac{-3 - \sqrt{q}}{2(2)}$ or better or $-\frac{3}{4} + \sqrt{\frac{57}{16}}$ oe or $-\frac{3}{4} - \sqrt{\frac{57}{16}}$ oe</p> <p>SC1 for -2.6 or $-2.637\dots$ and 1.1 or $1.137\dots$ or -2.64 and 1.14 seen in working or 2.64 and -1.14 as final answers</p>
<p>6 (a) (i)</p> <p>(ii)</p> <p>(b)</p>	<p>27</p> <p>3.89 or 3.888 to 3.889</p> <p>76 cao</p>	<p>1</p> <p>2</p> <p>3</p>	<p>M1 for $\frac{7}{EZ} = \frac{9}{5}$ oe</p> <p>B2 for $ABC = 104$ or $AOC = 152$ or $COD = 28$ or $OBA = 52$ and $OBC = 52$ or $BCD = 128$ and $OCB = 52$ or B1 for any one of $OBA, OBC, OCB = 52$ or $BCD = 128$</p>

Question	Answer	Marks	Part Marks
(c) (i)	90	1	
	angle in semicircle	1	
(ii)	27	1	
	tangent [perpendicular to] radius	1	
(iii)	rectangle	1	
7 (a)	72.7 or 72.70 to 72.71 nfw	4	M1 for midpoints soi (condone 1 error or omission) (47.5, 55, 65, 80, 95, 110) M1 for use of $\sum fx$ with x in correct interval including both boundaries (condone 1 further error or omission) (1092.5, 3520, 7930, 10880, 2470, 3190) M1 (dep on 2nd M1) for $\sum fx \div 400$
(b) (i)	[23] 87 209 345 371 [400]	2	B1 for 2 or 3 correct
(ii)	Correct graph	3	B1FT <i>their</i> (b)(i) for 6 correct heights B1 for 6 points at upper ends of intervals on correct vertical line B1FT (dep on at least B1) for increasing curve or polygon through 6 points After 0 scored, SC1FT <i>their</i> (b)(i) for 5 correct points plotted
(iii) (a)	69 to 70	1	
(b)	20 to 23	2FT	FT <i>their</i> cumulative freq curve M1 for correct UQ or LQ for <i>their</i> cumulative freq curve
(c)	72 to 75	2	M1 for 240 soi
8 (a) (i)	5.14 or 5.135 to 5.142 nfw	4	M2 for $[XY^2 =] 12.5^2 + 9.9^2 - 2 \times 12.5 \times 9.9 \times \cos 23$ or M1 for implicit version A1 for 26.4 to 26.5 OR B1 for $[XYT =] 108$ or $[TXY =] 49$ M2 for $\frac{12.5 \sin 23}{\sin(180 - 72)}$ oe or M1 for $\frac{\sin(180 - 72)}{12.5} = \frac{\sin 23}{XY}$ oe

Question	Answer	Marks	Part Marks
(ii)	15.6 or 15.7 or 15.64 to 15.68	3	M2 for $[TZ=]\frac{9.9}{\sin 37} \times \sin(72)$ oe or M1 for $\frac{9.9}{\sin 37} = \frac{TZ}{\sin 72}$ oe OR M2 for $\frac{12.5 \times \sin(180 - 23 - 108)}{\sin 37}$ oe or M1 for $\frac{\sin 37}{12.5} = \frac{\sin(180 - 23 - 108)}{TZ}$ oe
(b)	3.79 or 3.793 to 3.794	4	M3 for $r = 20.5 \div \left(2 + \frac{3 \times 65 \times 2\pi}{360}\right)$ oe or M2 for $20.5 = 2r + \frac{3 \times 65}{360} \times 2\pi r$ oe or M1 for $[3 \times] \frac{65}{360} \times 2\pi r$ oe or $20.5 = 2r +$ expression involving π
9 (a)	$x < 10$ oe $y \geq 2$ oe	1 1	Accept $x \leq 9$ Accept $y > 1$
(b)	$x + 3y \leq 21$ oe	1	Mark answer line isw
(c)	ruled broken line $x = 10$ ruled line $y = 2$ ruled line from (0, 7) to (21, 0) correct region indicated cao	B1 B1 B2 1	or ruled line $x = 9$ or ruled broken line $y = 1$ SC1 for line with negative gradient correct only at (0, 7) or (21, 0)
(d) (i)	4	1	
(ii)	20	1	
10 (a) (i)	$(6 - 2) \times 180$ or $(2 \times 6 - 4) \times 90$ or $(360 \div 6)$ $(6 - 2) \times 180 \div 6$ or $(2 \times 6 - 4) \times 90 \div 6$ or $180 - (360 \div 6)$	M1 M1dep	dep on previous M1
(ii)	$1.73x$ or $x\sqrt{3}$ oe	3	M2 for $2x \sin 60$ or $2x \cos 30$ oe or for $\sqrt{x^2 + x^2} - 2 \times x \times x \times \cos 120$ or M1 for $x \sin 60$ or $x \cos 30$ oe or for $x^2 + x^2 - 2 \times x \times x \times \cos 120$

Question	Answer	Marks	Part Marks
(iii)	$(10 - x)\sin 30$ seen oe	M1	
	$10 + 2((10 - x)\sin 30)$ oe	M1dep	dep on previous M1
	$10 + 10 - x$ or $10 + 2 \times \frac{1}{2} \times (10 - x)$	A1	with no errors or omissions seen
(b)	12.7 or 12.67 to 12.68.... nfw	4	B3 for 7.32 to 7.33 or M2 for $x = 20 \div (1 + 1.73)$ oe or M1 for $20 - x = \textit{their (a)(ii)}$ oe
11 (a)	4 5 6 7 8 16 32 64 128	1 3	B2 for 3 or 4 correct or B1 for first 2 correct If 0 scored, SC1 for 4 values correctly doubled FT one error
(b)	2^n oe	1	
(c) (i)	$2 + 4 + 8 = 14$ $16 - 2 = 14$	1 1	or for $14 + 2 = 16 = 2^4$
(ii)	62 and 6	2	B1 for each
(iii)	$2^{n+1} - 2$ oe	1	
(iv)	9	1	